# An Empirical Analysis of Pruning Techniques

Performance, Retrievability and Bias



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## What is the Relationship between Retrieval Effectiveness, Efficiency and Bias?

#### **Research Questions**

When an inverted index is optimized...

- How does the retrieval bias of an IR system change?
- What is the relationship between performance and bias?

#### What is Retrieval Bias?

Retrievability  $\mathbf{r}$  of a document  $\mathbf{d}$  with respect to the configuration of an IR system is defined as (Azzopardi and Vinay, 2008):

$$\mathbf{r}(\mathbf{d}) \propto \sum\nolimits_{\mathbf{q} \in \mathbf{Q}} \mathbb{I}(\mathbf{k_{dq}} \leq \mathbf{c}) \times 1/\mathbf{k_{dq}^{\beta}}$$

where  $\mathbf{k}_{dq}$  is the rank at which d is retrieved given q, c is a predefined threshold, and  $\beta$  is a hyperparameter. The Gini Coefficient is used to measure the retrieval bias of the system on the population of documents.

### **Experiment Setup**

#### **Retrieval System**

- Indri index over GOV2 (25M docs/39M unique terms)
- All documents Krovetz-stemmed and stopwords removed
- Retrieval using optimized BM25:  $k_1 = 0.9$  and b = 0.4
- Effectiveness measured over TREC Topics 701-850

#### **Static Index Pruning Methods**

- TCP: Term-based pruning (Carmel et al., 2001)
- DCP: Document-centric pruning (Büttcher and Clarke, 2006)
- UP: Uniform pruning (Carmel et al., 2001; Chen and Lee, 2013)
- REN: Rényi divergence of order infinity (Chen et al, 2015)

Comparisons are made between prune ratios  $0.1, 0.2, \ldots, 0.9$ .

## Main Results

#### Relationship between Performance, Efficiency and Retrieval Bias

- A lower Gini score indicates less bias, and a lower RSUM score (i.e.  $\sum_{d} r(d)$ ) indicates that less documents are retrievable.
- Bias remains stable until a turning point, between prune ratio 0.3–0.7 depending on the pruning algorithm, after which bias increases.
- DCP and REN appear to give a better trade-off than TCP.
- Selecting prune ratio based on the Gini score would result in good pruning performance without a sizable loss in early precision.



#### **Interaction between Performance and Retrieval Bias**

- The star indicates the "starting point" (un-pruned index), and each subsequent point corresponds to an 0.1 increase in the prune ratio.
- For UP, DCP and REN, performance tends to improve as bias decreases (i.e. less bias ⇒ better performance), but for TCP the relationship appears more complex.

